

II B. Tech II Semester Regular/Supplementary Examinations, July- 2023

FORMAL LANGUAGES AND AUTOMATA THEORY

(Common to CSE, CST, CSE(AIML), CSE(AI), CSE(DS), CSE(AIDS), CSE(CS), CSE(IOTCSIBCT),
CSE(IOT), AIML, CS, AIDS, CS& AIML)

Time: 3 hours

Max. Marks: 70

Answer any **FIVE** Questions each Question from each unit
All Questions carry **Equal** Marks

UNIT-I

- 1 a) Construct DFA equivalent to the given NFA [7M]

	0	1
$\rightarrow A$	{A,B}	A
B	C	C
C	D	Φ
\textcircled{D}	D	D

- b) Construct a DFA accepting the set of all strings ending with 'bb' over
- $\Sigma=\{a,b\}$
- . [7M]

Or

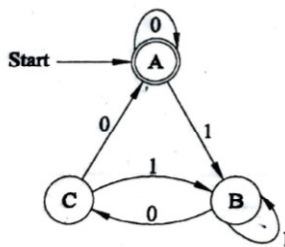
- 2 a) Draw the transition diagram of a FA which accepts all strings of 0's and 1's in which the number of 0's are odd and 1's are even. [7M]

- b) Construct the moore machine to determine residue mod 3 . [7M]

UNIT-II

- 3 a) Apply pumping lemma for the language
- $L=\{a^n/n \text{ is prime}\}$
- and prove that it is not regular. [7M]

- b) Write equivalent regular expression for the following DFA. [7M]



Or

- 4 a) Give regular expression for representing the set L of strings in which every 0 is immediately followed by at least two 1's . [7M]

- b) Construct the left linear grammar for the language
- $(0+1)^*00(0+1)^*$
- [7M]

UNIT-III

- 5 a) Write CFG for the language $L = \{0^n 1^n | n \geq 1\}$ i.e. the set of all strings of one or more 0's followed by an equal number of 1's. [7M]
- b) Eliminate NULL productions for the grammar [7M]
- $$S \rightarrow ABC | BaB$$
- $$A \rightarrow aA | BaC | aaaa$$
- $$B \rightarrow bbb | a | D$$
- $$C \rightarrow CA | AC$$
- $$d \rightarrow \epsilon$$

Or

- 6 a) Prove that the following grammar is ambiguous on the string 'aab' [7M]
- $$S \rightarrow aS | aSb | S\epsilon$$
- b) Find the GNF equivalent to the following [7M]
- $$S \rightarrow AA | 0$$
- $$A \rightarrow SS | 1$$

UNIT-IV

- 7 a) Design Push Down Automata for $L = \{a^{2n} b^n | n \geq 1\}$ [7M]
- b) Convert the following Context Free Grammar to Push Down Automata [7M]
- $$S \rightarrow aA | bB$$
- $$A \rightarrow aB | a$$
- $$B \rightarrow b$$

Or

- 8 Construct the equivalent grammar for the PDA [14M]
- $$M = (\{q_0, q_1\}, \{0, 1\}, \{R, Z_0\}, \delta, q_0, Z_0, \Phi)$$
- and δ is given by
- $$\delta(q_0, 0, Z_0) = (q_0, RZ_0)$$
- $$\delta(q_0, 0, R) = (q_0, RR)$$
- $$\delta(q_0, 1, R) = (q_1, R)$$
- $$\delta(q_1, 1, R) = (q_1, R)$$
- $$\delta(q_1, 0, R) = (q_1, \epsilon)$$
- $$\delta(q_1, \epsilon, Z_0) = (q_1, \epsilon)$$

UNIT-V

- 9 a) Design a Turing Machine to accept $L = \{WW^R | W \text{ is in } (a+b)^*\}$ [7M]
- b) Construct Turing Machine to compute the function \log_2^n [7M]

Or

- 10 a) Write short note on NP- hard and NP- complete problem. [7M]
- b) Check whether the following post correspondence problem has a solution or not. [7M]

I	List A	List B
1	10	11
2	1001	001
3	100	101

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**UNIT-I**

- 1 a) Design NFA accepting string with a's and b's such that string containing two consecutive a's or two consecutive b's. [7M]
- b) Briefly discuss about Finite Automata with Epsilon- Transition. [7M]

**Or**

- 2 a) Check whether the following two FSM's are equivalent or not. [7M]

|    |   |   |
|----|---|---|
| M1 | 0 | 1 |
| →A | B | D |
| ⓑ  | A | C |
| C  | D | B |
| ⓓ  | C | A |

|    |   |   |
|----|---|---|
| M2 | 0 | 1 |
| →P | R | R |
| Q  | R | P |
| Ⓡ  | P | Q |

- b) Draw the transition diagram of a FA which accepts all strings of 0's and 1's in which the number of 0's are even and 1's are odd. [7M]

**UNIT-II**

- 3 a) Write a R.E. for the following DFA. [7M]

|    |   |   |
|----|---|---|
|    | a | b |
| →P | Q | P |
| Ⓚ  | Q | P |

- b) Construct a Regular grammar G generating the regular set represented by  $a^*b(a+b)^*$  [7M]

**Or**

- 4 a) Construct NFA with  $\epsilon$  transition for the following expression  $0^* + 11$  [7M]
- b) Construct the right linear grammar for the language  $(01)^*0$  [7M]

## UNIT-III

- 5 a) Define Context free grammar and write context free grammar for the language  $L = \{a^i b^j c^k \mid i+j=k, i \geq 0, j \geq 0\}$  [7M]
- b) Eliminate Null, unit and useless production from the following grammar [7M]
- $$\begin{aligned} S &\rightarrow AaA|CA|BaB \\ A &\rightarrow aaBa|CDAlaalDC \\ B &\rightarrow bB|bAB|bbaS \\ C &\rightarrow CalbCID \\ D &\rightarrow bD|\epsilon \end{aligned}$$

Or

- 6 a) Define ambiguous Grammar. Prove that the following grammar is Ambiguous. [7M]
- $$S \rightarrow aS|aSbS|\epsilon$$
- b) Convert the following CFG to CNF [7M]
- $$\begin{aligned} S &\rightarrow ASB|\epsilon \\ A &\rightarrow aAS|a \\ B &\rightarrow SbS|A|bb \end{aligned}$$

## UNIT-IV

- 7 a) Construct PDA for the language  $L = \{a^m b^m c^n \mid m, n \geq 1\}$  [7M]
- b) Construct PDA equivalent to the following CFG [7M]
- $$\begin{aligned} S &\rightarrow 0A \\ A &\rightarrow 0ABC \mid 1B \mid 0 \\ B &\rightarrow 1 \\ C &\rightarrow 2 \end{aligned}$$

Or

- 8 Construct the CFG for the PDA [14M]
- $M = (\{q_0, q_1\}, \{0, 1\}, \{R, Z_0\}, \delta, q_0, Z_0, \Phi)$  and  $\delta$  is given by
- $$\begin{aligned} \delta(q_0, 1, Z_0) &= (q_0, RZ_0) \\ \delta(q_0, 1, R) &= (q_0, RR) \\ \delta(q_0, 0, R) &= (q_1, R) \\ \delta(q_1, 0, Z_0) &= (q_0, Z_0) \\ \delta(q_0, \epsilon, Z_0) &= (q_0, \epsilon) \\ \delta(q_1, 1, R) &= (q_1, \epsilon) \end{aligned}$$

## UNIT-V

- 9 a) Design a TM to recognize the language  $L = \{1^n 2^n 3^n \mid n \geq 1\}$  [7M]
- b) Design TM which will recognize strings containing equal number of a's and b's [7M]
- Or
- 10 a) Describe various ways of representing Turing machines with suitable examples. [7M]
- b) What is meant by Turing Reducibility? Explain. [7M]

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**Time: 3 hours**

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Answer any **FIVE** Questions each Question from each unit  
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UNIT-I

- 1 a) Construct NFA with ϵ which accepts a language consisting the strings of any no. of 0's followed by any no. of 1's followed by any no. of 2's. And also convert into NFA without ϵ [7M]
- b) Draw the transition diagram of a FA which accepts all strings of 0's and 1's in which the number of 0's are even and 1's are even. [7M]
- Or**
- 2 a) Design a Mealy machine which can output symbols 'E' or 'O' according to the total number of 1's encountered is even or odd. The input symbols are 0 and 1. [7M]
- b) Construct the minimum state equivalent DFA [7M]

	0	1
$\rightarrow A$	B	A
B	A	C
C	D	B
D	D	A
E	D	F
F	G	E
G	F	G
H	G	D

UNIT-II

- 3 a) State pumping lemma for regular languages. Prove that the following language $L = \{ a^n b^n \mid n \geq 1 \}$ is not a regular. [7M]
- b) Prove the following identity $(a^*ab + ba)^*a^* = (a + ab + ba)^*$ [7M]
- Or**
- 4 a) Construct the right linear grammar for the language $(0+1)^*00(0+1)^*$ [7M]
- b) Describe the following sets by regular expressions [7M]
- i) the set of all strings of 0's and 1's beginning with 00.
- ii) the set of all strings of 0's and 1's beginning with 1 and ending with 00.

UNIT-III

- 5 a) Define Context free grammar and write context free grammar for the language $L = \{a^n b^m c^k \mid n+2m=k\}$ [7M]
 b) Remove all useless Symbols and all ϵ – productions from the grammar [7M]
 $S \rightarrow aA|aB$
 $A \rightarrow aaA|B|\epsilon$
 $B \rightarrow b|bB$
 $D \rightarrow B$

Or

- 6 a) Consider the grammar $S \rightarrow aS/aSbS/\epsilon$ [7M]
 Is the above grammar ambiguous?
 Show in particular that the string 'aab' has to :
 i. parse tree ii. Leftmost derivation iii. Rightmost derivation
 b) Convert the following grammar to Greibach Normal Form [7M]
 $S \rightarrow ABA \mid AB \mid BA \mid AA \mid B$
 $A \rightarrow aA \mid a$
 $B \rightarrow bB \mid b$

UNIT-IV

- 7 a) Design a PDA for the language $L = \{w \mid w \in (0+1)^* \text{ and no.of } 0\text{'s} < \text{no.of } 1\text{'s}\}$ [7M]
 b) Convert the following Context Free Grammar to Push Down Automata [7M]
 $S \rightarrow 0AA$
 $A \rightarrow 0S \mid 1S \mid 0$

Or

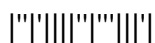
- 8 Construct the CFG for the PDA $M = (\{q_0, q_1\}, \{0, 1\}, \{R, Z_0\}, \delta, q_0, Z_0, \Phi)$ and δ is [14M]
 given by

$$\begin{aligned} \delta(q_0, 1, Z_0) &= (q_0, RZ_0) \\ \delta(q_0, 1, R) &= (q_0, RR) \\ \delta(q_0, 0, R) &= (q_1, R) \\ \delta(q_1, 0, Z_0) &= (q_0, Z_0) \\ \delta(q_0, \epsilon, Z_0) &= (q_0, \epsilon) \\ \delta(q_1, 1, R) &= (q_1, \epsilon) \end{aligned}$$

UNIT-V

- 9 a) Design a TM to recognize the language $L = \{0^n 1^n 0^n \mid n \geq 1\}$ [7M]
 b) Write a short note on linear bounded automata. [7M]
- Or
- 10 a) What are undecidable problems? Explain with example. [7M]
 b) Check whether the following post correspondence problem has a solution or not. [7M]

I	List A	List B
1	111	11
2	1001	01
3	1110	1001



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Answer any **FIVE** Questions each Question from each unit
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UNIT-I

- 1 a) Convert the following NFA with ϵ to equivalent DFA [7M]

	0	1	ϵ
$\rightarrow A$	Φ	A	B
B	B	Φ	C
\textcircled{C}	B	A	Φ

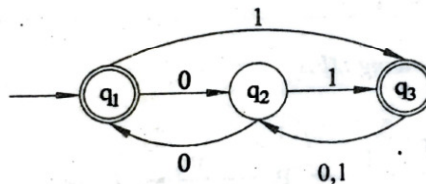
- b) Draw the transition diagram of a FA which accepts all strings of 0's and 1's in which the number of 0's are odd and 1's are odd. [7M]

Or

- 2 a) Construct the minimum state automata for the following. [7M]

	0	1
$\rightarrow A$	B	C
B	B	C
C	B	C
D	B	E
\textcircled{E}	B	C

- b) Obtain a regular expression for the following FA [7M]



UNIT-II

- 3 a) Show that $L = \{ 0^i 1^j \mid \gcd(i,j) = 1 \}$ is not regular. [7M]
 b) Write equivalent regular expression for the following DFA. [7M]

δ	0	1
$\rightarrow q_1$	q_2	q_3
q_2	q_3	q_1
q_3	q_2	q_2

Or

- 4 a) Find the regular expression for the Language $L = \{ a^{2n} b^{2m} \mid n \geq 0, m \geq 0 \}$ [7M]
 b) Simplify the following R.E. $r = \epsilon + a^*(abb)^*(a^*(abb)^*)^*$ [7M]

UNIT-III

- 5 a) Write CFG for the language $L = \{ a^n b^n \mid n \geq 1 \}$ i.e. the set of all strings of one or more a's followed by an equal number of b's [7M]
 b) Using CFL pumping lemma show that the following language is not context free [7M]
 $L = \{ a^i b^j c^k \mid i < j < k \}$

Or

- 6 a) What is an ambiguous grammar? Show that the following grammar is ambiguous, where E is the start symbol. [7M]
 $E \rightarrow E + E \mid E - E \mid E * E \mid E / E \mid (E) \mid a$

- b) Convert the following CFG to CNF [7M]
 $S \rightarrow ASB \mid \epsilon$
 $A \rightarrow aAS \mid a$
 $B \rightarrow SbS \mid A \mid bb$

UNIT-IV

- 7 a) Construct PDA for the language $L = \{ a^{2m} b^m c^n \mid m, n \geq 1 \}$ [7M]
 b) For the following grammar construct a PDA [7M]
 $S \rightarrow aABB \mid aAA$
 $A \rightarrow aBB \mid a$
 $B \rightarrow bBB \mid A$
 $C \rightarrow a$

Or

- 8 a) Describe the steps in conversion of a CFG to a PDA with a suitable example. [7M]
 b) Compare and contrast PDA with two stack PDA. [7M]

UNIT-V

- 9 a) Design a TM to accept the language $L = \{ wcw^R \mid w \in (a+b)^* \}$ [7M]
b) Define a Turing Machine. Give its classification with suitable examples. [7M]
- Or**
- 10 a) Write a short note on Church's hypothesis. [7M]
b) Briefly explain about post's correspondence problem. [7M]

